Section I 10 marks Attempt Questions 1-10 Allow about 15 minutes for this section

Use the multiple choice answer sheet for Questions 1 - 10.

- 1 Convert the angle measurement 76° into radians correct to 3 significant figures.
 - (A) 7.6
 - (B) 1.33
 - (C) 1.326
 - (D) 0.422
- 2 Which of the following is a factorisation of the expression $x^2 2 + \frac{1}{x^2}$?

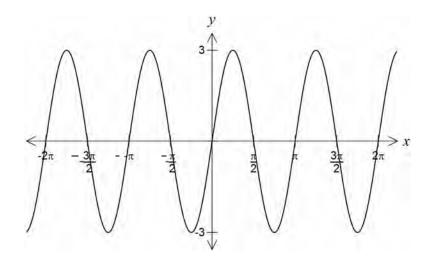
(A)
$$\left(x - \frac{1}{x}\right)\left(x + \frac{1}{x}\right)$$

(B) $\left(x + \frac{1}{x}\right)^2 - 2$
(C) $\left(x - \frac{1}{x}\right)^2$
(D) $\left(x + \frac{2}{x}\right)\left(x - \frac{1}{x}\right)$

3 What is the value of
$$\lim_{x\to 3} \left(\frac{x^2-9}{x-3}\right)$$
?

- (A) 6
- (B) 0
- (C) 1
- (D) undefined
- 4 A parabola has the equation $(y-1)^2 = 8(x+2)$. Which of the following is the correct statement?
 - (A) The vertex is (-2,1) and the focus is (0,1)
 - (B) The vertex is (1, -2) and the focus is (3, -2)
 - (C) The vertex is (1, -2) and the focus is (-1, -2)
 - (D) The vertex is (-2,1) and the focus is (-4,1)

5 Consider the graph of f(x) shown,



Which of the following functions describes f(x)?

- (A) $f(x) = 3\cos x$
- (B) $f(x) = 3 \cos 2x$
- (C) $f(x) = 3 \sin 2x$
- (D) $f(x) = 3 \sin x$

$$\mathbf{6} \quad \frac{d}{dx}(\sin 2x) =$$

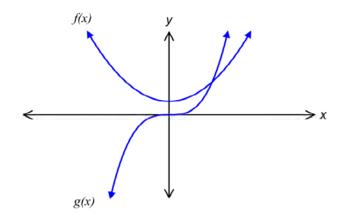
- (A) $2\sin 2x$
- (B) $2\cos 2x$
- (C) $2 \tan 2x$

(D)
$$\frac{1}{2}\cos 2x$$

7 What is the value of
$$\sum_{r=1}^{50} (2r-4)$$
?

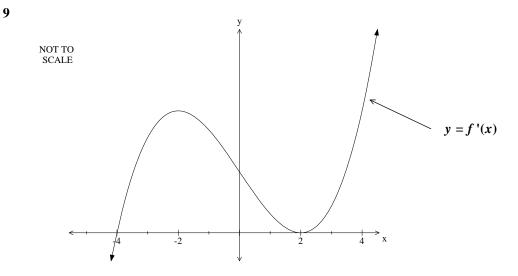
- (A) 96
- (B) 2350
- (C) 2450
- (D) 4700

8 Consider the functions f(x) and g(x) shown on the same pair of axes below:



Which statement is true?

- (A) f(x) and g(x) are both even functions.
- (B) f(x) and g(x) are both odd functions.
- (C) f(x) is an even function and g(x) is an odd function.
- (D) f(x) and g(x) are both neither odd nor even functions.



The diagram above represents a sketch of the **gradient function** of the curve y = f(x). Which of the following is a true statement ? For the curve y = f(x)

- (A) a horizontal point of inflexion occurs at x = -4
- (B) a horizontal point of inflexion occurs at x = 2
- (C) a maximum turning point occurs at x = -2
- (D) a maximum turning point occurs at x = 2

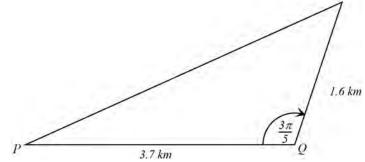
- 10 A quadratic equation has roots α and β . If $\alpha + \beta = 6$ and $\alpha \beta = 4$, the quadratic equation could be written as
 - (A) $x^2 6x + 13 = 0$
 - (B) $-x^2 + 6x 5 = 0$
 - (C) $3x^2 18x + 4 = 0$
 - (D) $2x^2 12x + 5 = 0$

END OF SECTION 1

Section II 90 marks Attempt Questions 11-16 Allow about 2 hours and 45 minutes for this section Answer each question in a separate writing booklet.

In Questions 11-16, your responses should include relevant mathematical reasoning and/or calculations.

Question 11 (15 marks) Use a SEPARATE writing booklet Marks (a) What is $\frac{1+\sqrt{5}}{7-2\sqrt{5}}$ as a fraction with a rational denominator? 1 (b) Differentiate with respect to *x* and simplify fully: (i) 2 x (ii) $5x(x^2-3)$ 2 (c) Find $\int \frac{x^2 + 3x}{x} dx$ 2 (d) If $f(x) = 2 \tan x$, find the exact value of $f'\left(\frac{\pi}{4}\right)$ 2 (e) A pendulum oscillates through a distance of 3 cm on the first swing, 2 cm on 2 the second swing, and on each successive swing through a distance of $\frac{2}{3}$ of the previous swing. How far will the pendulum travel before coming to a rest? For triangle POR, (f) R



(i)Find the length of *PR* correct to 1 decimal place.2(ii)Using the sine rule, find the size of $\angle R$ in radians, correct to 3
significant figures.2

End question 11

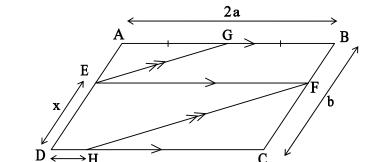
Question 12 (15 marks) Use a SEPARATE writing booklet					
(a)	(a) Solve $x^2 - 5x > 0$				
(b)	The length of an arc of a circle with radius 5cm is 14cm. Find the angle subtended at the centre by the arc. Give your answer to the nearest minute.				
(c)	How many terms of the arithmetic sequence 66, 62, 58, are positive?				
(d) Graph on a number line the values of x for which $ x-2 \le 1$.					
(e)	Find the equation of the tangent to the curve $y = x^2 - 5x$ at the point $(1, -4)$.				
(f)	Top soil is tipped from a truck onto a pile. The rate, $R \text{ kg/s}$, at which the top soil is flowing is given by the expression $R = t(100 - t^2)$ for $0 \le t \le A$, where <i>t</i> is the time in seconds after the top soil begins to flow.				
	(i) What is the rate of flow after 5 seconds?	1			
	(ii) What is the largest value of <i>A</i> for which the expression for <i>R</i> is physically reasonable?	1			
	(iii) Find the maximum rate of flow of the top soil.	3			

End question 12.

(a) The perpendicular distance from the point (1, 3) to the line x - y + c = 0is $\frac{5}{\sqrt{2}}$. Find the possible value(s) of *c*.

- (b) A group of students decided to monitor the population of squirrels in a park. Initially there were 49 squirrels in the park. The population, P, of squirrels, after *t* weeks is given by $P=49e^{kt}$
 - (i) After 7 weeks the population of squirrels has doubled. 2 Show that $k = \frac{\ln 2}{7}$.
 - (ii) During which week did the population of squirrels exceed 180? 2
 - (iii) What is the rate of change of the population of squirrels per week, after 14 weeks?
- (c) ABCD is a parallelogram with sides AB = 2a and BC = b and DE = x. EF is parallel to AB and DC.

G is the midpoint of *AB*. The line parallel to EG from F intersects *CD* at *H* where DH = m.



- (i) Show that $\triangle AEG$ is similar to $\triangle CFH$. 2
- (ii) Find an expression for x in terms of a, b and c.

m

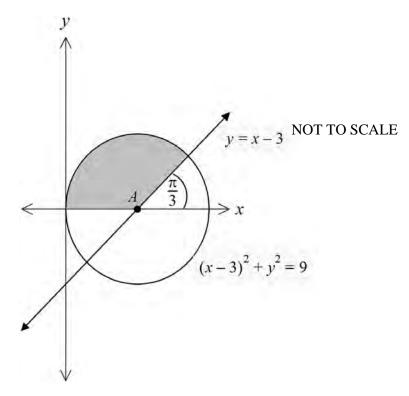
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Question 13 continued next page

2

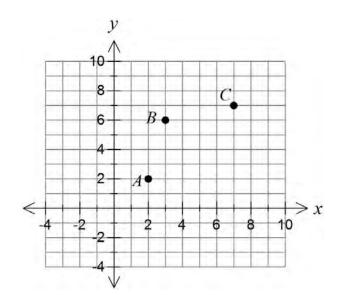
2

(d) The diagram shows the graphs $(x-3)^2 + y^2 = 9$ and y = x-3. The point *A* is the centre of the circle.



(i)	Write down inequalities that describe the sector that is shaded in the diagram.	1
(ii)	Find the exact area of the shaded sector.	2

End question 13



(i)	Find the coordinates of point <i>D</i> .	1
(ii)	Find the exact length of the diagonal AC.	1
(iii)	Find the point of intersection of the diagonals AC and BD.	1
(i) Pro	ove that $\frac{2 \cot A}{2(\csc^2 A) - 2} = \tan A$	2

(ii) Hence or otherwise solve
$$\frac{2 \cot A}{2(\csc^2 A) - 2} = \sqrt{3}$$
 for $0 \le A \le 2\pi$.

$$\dot{x} = b + \frac{c}{t+1}$$
 where b and c are constant.

Given that the particle has initial velocity 2ms^{-1} and its initial acceleration was 4ms^{-2} , find the values of *b* and *c*.

Question 14 continued next page

(b)

Question 14 (continued)

(d) A function is given by $f(x) = x^2 - \frac{x^3}{9}$.

(i)	Find the coordinates of the stationary points of $y = f(x)$ and determine their nature.	3
(ii)	Hence, sketch the graph of $y = f(x)$ for $-3 \le x \le 12$ showing the stationary points.	2

(iii) Find the maximum value of
$$y = -f(x)$$
 for $-3 \le x \le 12$. 1

End question 14

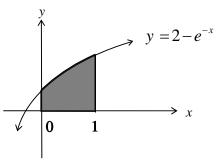
CTHS Mathematics Trial 2013 - AP4

Marks

(a) State the range of $y = \sqrt{4 - x^2}$.

(b) Find the value of q, given that
$$\int_{q}^{\frac{2\pi}{3}} \cos\left(\frac{x}{2}\right) dx = \sqrt{3} - \sqrt{2} .$$
 3

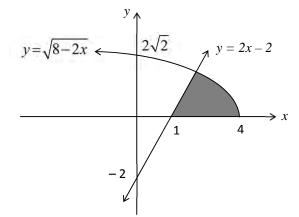
(c) The region shaded in the diagram is bounded by $y = 2 - e^{-x}$, the x-axis, the y-axis and the line x = 1.



Find the exact volume of the solid formed when the shaded region is rotated about the *x*-axis.

(d) In the diagram, the line y = 2x - 2 intersects the curve $y = \sqrt{8 - 2x}$ at the point *P*.

The region bounded by this line, the curve $y = \sqrt{8-2x}$ and the x-axis is shaded as shown on the diagram.



- (i) Find the *x* coordinate of the point *P*.
- (ii) Find the area of the shaded region.

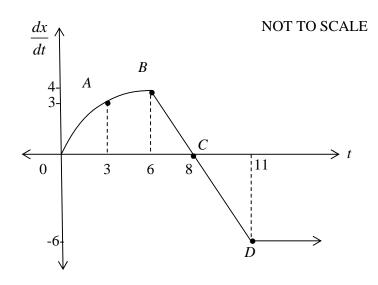
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Question 15 continued next page

1

3

the object, as a function of time, *t*. The coordinates of the points shown on the graph are *A* (3, 3), *B* (6, 4), *C* (8, 0) and *D* (11, -6). The object is initially at the origin and the velocity is constant at -6m/s for $t \ge 11$.



(i) Use the Trapezoidal rule with 3 function values to calculate the distance travelled by the object between t = 0 and t = 6.

(ii)	Find the displacement of the object when $t = 11$.	1

(iii) During which time(s) is the object slowing down? 1

End Question 15

Question 16 (15 Marks) Use a SEPARATE writing booklet

- (a) Given that f''(x) = 2, find the equation of a curve y = f(x) which has a stationary point at the point (1,3).
- (b) Jack opened an investment account with an initial deposit of \$5000 on 1st January 2007. He did this so that he could provide his daughter with \$800 at the start of January each year for university text books. The account earned interest at a rate of 3% per annum, compounding annually and paid at the end of each year.

The first \$800 withdrawal was made one year after the investment was set up.

- (i) Calculate the account balance immediately after the first withdrawal **1** has been made.
- (ii) Let A_n be the amount of money in the account after *n* years (when *n* **2** withdrawals will have been made).

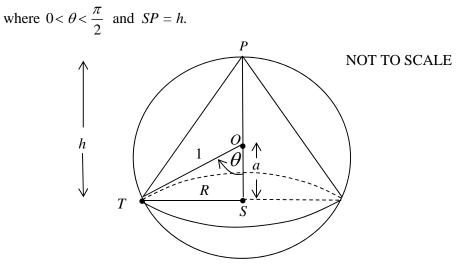
Show that $A_n = \frac{1}{3} \left[80000 - 65000(1.03)^n \right]$.

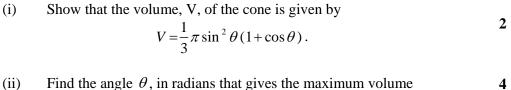
(iii) After withdrawing \$800 on 2ndJanuary 2010, Jack's daughter advised **3** him that she would need \$900 per year from 2011 onwards.

How many more years of textbook fees can come out of the fund?

Question 16 continued next page

(c) The diagram below shows a cone of radius, R, and height, h, inscribed in a sphere with a radius of 1cm and centre at O. The distance, a, is from the centre of the sphere to the base of the cone. OT is inclined at angle θ from SO,





(ii) Find the angle θ , in radians that gives the maximum volume of the cone.

End of paper

Student Name	 	
Class		

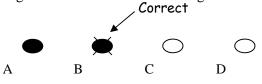
Select the alternative A, B, C or D that best answers the question. Fill in the response oval completely.

Sample: 2 + 4 = (A) 2 (B) 6 (C) 8 (D) 9 A \bigcirc B \bigcirc C \bigcirc D \bigcirc

• If you think you have made a mistake, put a cross through the incorrect answer and fill in the new answer.



• If you change your mind and have crossed out what you consider to be the correct answer, then indicate the correct answer by writing the word correct and drawing an arrow as follows.



1.	A ()	B 🔿	C O	D 🔿
2.	A ()	вO	сО	D O
3.	A ()	B ()	сО	D O
4.	$_{\rm A}$ \bigcirc	вO	сО	D O
5.	$A \bigcirc$	вO	сO	D O
6.	$A \bigcirc$	вO	сО	D O
7.	$A \bigcirc$	вO	сO	D O
8.	$A \bigcirc$	вO	сO	D O
9.	$A \bigcirc$	вO	сO	D O
10.	$A \bigcirc$	вO	с О	DО

$$\frac{7244k}{1.6} = 20/3 = 50 \text{ LUTION TO THE ALL STATES AND THE ALL ST$$

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$$\frac{\partial ueschion ||}{\partial u} = \frac{1+\sqrt{5}}{7-2\sqrt{5}} \times \frac{7+2\sqrt{5}}{7+2\sqrt{5}}$$

$$= 7+2\sqrt{5} + 7\sqrt{5} + 10$$

$$= 17 + 9\sqrt{5}$$

$$\frac{\sqrt{29}}{29}$$

$$\frac{\sqrt{29}}{29}$$

$$\frac{\sqrt{29}}{\sqrt{29}}$$

$$\frac{\sqrt{29}}{\sqrt{29}$$

$$d). \quad f(x) = 2 \tan x$$

$$J'(x) = 2 \det^{2} x$$

$$J'(x) = 2 \det^{2} x$$

$$J'(x) = 2 \det^{2} x$$

$$= 2 (\sqrt{2})^{2}$$

$$= 4 \cdot \cdot$$

$$\left(\frac{\operatorname{hofz}}{\sqrt{2}} = \frac{1}{\sqrt{2}} + \frac{\sqrt{2}}{\sqrt{1}} \right)$$

$$= 2 \cdot (\sqrt{2})^{2}$$

$$= 4 \cdot \cdot$$

$$\left(\frac{\operatorname{hofz}}{\sqrt{2}} = \frac{1}{\sqrt{2}} + \frac{\sqrt{2}}{\sqrt{1}} \right)$$

$$= 2 \cdot (\sqrt{2})^{2}$$

$$= 4 \cdot \cdot$$

$$\left(\frac{\operatorname{hofz}}{\sqrt{2}} = \frac{1}{\sqrt{2}} + \frac{\sqrt{2}}{\sqrt{1}} \right)$$

$$= 2 \cdot (\sqrt{2})^{2}$$

$$= 4 \cdot \cdot$$

$$\operatorname{hofz}$$

$$\int x^{2} = \frac{3}{\sqrt{2}} + \frac{1}{\sqrt{2}} + \frac{1$$

.

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AP4 2013 Question 12 $d) |z-z| \leq l$ a) x2-5×>0 ~(x-5) >0 ie -1 ≤ x-2 ≤1 31 1 < 2 < 3 1. x<0 or x>5 A $y = x^2 - 5x$ e) y' = 2x - 5l=ro b) 5/ 14 = 50 at x = 1 $y' = 2 \times 1 - 5$ = -3 (= m) $\theta = \frac{14}{5} \times \frac{180}{T}$ equation of tangent y + 4 = -3(x - 1). = 160.42818 = 160° 26' y+4 = -3x+3 : 3x+y+1 = 0 c) 66, 62, 58.... a=66 d=-4 Tn>0 $T_n = a + (n - i)d$ f).i) $k = t(100 - t^2)$ when t=5 = 66 - 4n +4 $R = 5 \left(100 - 25 \right)$ = 70 - 44 = 5×75 for Th>0 70-41>0 , = 375 Kg/sec. 70>44 ii) & initially no for 17.5 > 11(when empty no flow. ". there are 17 positive terms to largest value of A when R=0 $\therefore o = f\left(100 - t^2\right)$ ie t=0 as t=10 hence largest values of tis 10 secs : A = 10

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And 12
fiii) max Rate of flow
when
$$dR = 0$$
 and
 $d^2R < 0.$
 $d^2R < 0.$
 dt^2
i. $dR = 100 - 3t^2$
 dt
for $dR = 0$ $0 = 100 - 3t^2$
 dt
 $t = 10$
 $\sqrt{3}$
as $t \ge 0$ $t = 10$
 $\sqrt{3}$ dec.
 $\frac{d^2R}{\sqrt{3}} = -6t$
 dt^2
 $at t = \frac{10}{\sqrt{3}}$ $d^2R = -6x10$
 $\sqrt{3}$
 dt^2
 dt^2

= 2000 353 max Rale of Alow. = 20005 kg/sec. 9

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$$\begin{aligned} & \mathcal{Q}_{Vestion} (3) \\ & x - q + c = 0 \qquad (1,3) \\ & a = 1 \ b = -1 \qquad diof = 5 \\ & \sqrt{12} \qquad (1 \times 1 - \sqrt{12} \times 3 + c) = 5 \\ & \sqrt{12} \qquad (1 \times 1 - \sqrt{12} \times 3 + c) = 5 \\ & \sqrt{12} \qquad (1 \times 1 - \sqrt{12} \times 3 + c) = 5 \\ & \sqrt{12} \qquad (1 \times 1 - \sqrt{12} \times 3 + c) = 5 \\ & \sqrt{12} \qquad (1 \times 1 - \sqrt{12} \times 3 + c) = 5 \\ & \sqrt{12} \qquad (1 \times 1 - \sqrt{12} \times 1 - c) = 5 \\ & \sqrt{12} \qquad (1 \times 1 - \sqrt{12} + c) = 5 \\ & \sqrt{12} \qquad (1 \times 1 - \sqrt{12} + c) = 5 \\ & c = 7 \\ & \sqrt{12} \qquad (1 \times 1 - \sqrt{12} + c) = 5 \\ & \sqrt$$

AP4 2013

Bu 13 cii) as DREG III DOFH Rate of change = de b iii) $\frac{dl}{dt} = 49 \, k e^{-kt}$ $= 49 \, \ln 2 e^{-14 \times \ln 2}$ 6-× ax = (b-x) (22-c) = 19.40812106 ax = 2ab - 2ax - bc + cx= 19.4 squirrels per week. : ax +2ax -cz = 2ab-bc $\chi(3a-c) = b(2a-c)$ c)ⁱ⁾ In DAEG and DCFH 2 *AEG = < FCH* (opposite <'s in a) parallelogram) $\chi = b(2a-c)$ 3a-c) LAGE = < GEF (alternate 25) AGIIEF d) i) y ≥0 (x -3)² + y LGEF = < EFH (alternate <'s EGIIHF) y ≥ ×· < EFH = < FHC (alternate <'s EF || DC 6 . - < AGE = < FHC i) Hence $< A = \overline{u} - \overline{u}$ DAEG III SCFH (equiangular) = 211 Area = 1 ro = 1 × 3 × 2 1 31 mits.

AR4 2013

Buesdion 14
a) i) by nispection from A
move 4 across and 1 up
D (6,3)
ii)
$$Ac = \sqrt{(7-2)^2 + (7-2)^2}$$

 $= \sqrt{50}$
 $= 5\sqrt{2}$ units

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iii) Diagonals of Khombus
bise et at right angles.

$$M = (7+2, 7+2)$$

$$= (4.5, 4.5)$$

b) i) LHS =
$$2 \cot A$$

 $2(\csc^2 A) - 2$
 $= 2 \cot A$
 $2(\csc^2 A - 1)$
 $= 2 \cot^2 A$
(: $\cot^2 A + 1 = \csc^2 A$)
 $= \frac{1}{\cot A}$
 $= 4 \tan A$
 $= RHS$.

$$\cot^2 A$$

 $\csc^2 A$)
 $+A$
 $+A$
 A
 HS .

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ii)
$$2 \cot A = \sqrt{3}$$

 $2(\csc A) - 2$
 $4 = \sqrt{3}$
 $A = \sqrt{$

Q14 20(3 a) $f(q) = \chi^2 - \chi^3$ \tilde{b} etation compositions i) f'(x) = 0 $-\frac{\chi^2}{\chi}=0$. . . 2x $x\left(2-\frac{x}{2}\right)=0$ 2-2=0 کح Z =0 2 3 2=6 2-2x \int_{1}^{α} (e) -50 J ~ (0 >0 (12, -48) f(12) $\int_{-12}^{4} (6) = 2 - \frac{12}{3}$ (-3,12) f(-3) $\int_{\Gamma} (9) = 0$ Max. Tui) y : Stationary pts fres Ō (\mathbf{I}) max 48 (00) -:0 a n. 2 has $y = 6^{2} - 6^{3}$ (6, 12)2 a (Jundion ¥ max =12 jlijo's)

Question 15 Ala 2013 =2-e ->x 05452. c) 111 $\int \frac{2\frac{1}{3}}{2} \cos(\frac{x}{2}) dx$ V= TI (y2 dre $= 2 \left[\frac{\sin x}{2} \right]^{\frac{24}{3}}$ $= 11 \left[4 - 4e + e^{-2x} + e^{-2x} \right]$ = II [4 7 + 4 e - e]] $= 2\left| \frac{\sin \pi}{3} - \sin \frac{9}{2} \right|$ $= \pi \left(\frac{5}{4} + \frac{4}{2} - \frac{1}{2} - \frac{5}{2} + \frac{1}{2} + \frac{1}{2} \right)$ fina $\sqrt{3}-\sqrt{2}=2\sqrt{3}$ $\binom{2}{2}$ $= \overline{11} \left\{ \begin{array}{c} 4 - 1 \\ e \end{array} \right\} + \frac{1}{2} \left\{ \begin{array}{c} -1 \\ -1 \end{array} \right\}$ 53-52 = J3 - 2 sin q $\frac{e^{R}}{11} \int \frac{e^{2} + 8e - 1}{2e^{2}} \int \frac{1}{12}$ $2 \sin q = \sqrt{2}$ di) 8-22 $\sin \frac{9}{2} = \sqrt{2}$ = 2x - 2=] 1 $8 - 2x = 4x^2 - 8x + 4$ $0 = 4x^2 - 6x - 4$ $\gamma = \overline{\mu}$ $0 = 2x^2 - 3x - 2$ $\mathcal{O} = (2x+1)(x-2)$ 9 = $\chi = -\frac{1}{2}, \chi = 2$ @R 1-57 Area = area A+ [J8-22 d $= \frac{1}{2} \cdot (1)(2) + \int_{1}^{4} (8 - 2\pi)^{\frac{1}{2}} d\pi$ $= 1 + \left(\frac{2}{3} \left(\frac{8}{-2x} \right)^{\frac{3}{2}} \right)^{\frac{3}{2}}$ $1 - \frac{1}{3} [0 - 8]$ 2 3 3 = 4 milts.

Qu 15 dii) or $\int_{1}^{2} 2x - 2 \, dx + \int_{2}^{4} \sqrt{8 - 4x} \, dx$ $= \left(2^{2} - 2x\right)^{2} + \left(-\frac{2}{3}\left(8 - 2x\right)^{3}\right)^{4}$ $= \frac{1}{2} \frac{3}{2} \frac{2}{2} u^2$. 15e) xn 0 3 6 h = 34 (i) <u>yn</u> o _3__ = [40 + 4n + 2 (41+42....)] Distance = $\frac{23}{2}\left[0+4+2(3)\right] = \frac{3}{2} \times 10$ = 15 metres. QISEN) Charge in Displacement = SV dt £x3x6 = 15+4-9 = 19 - 9 = 10 Since object is inhally at the particle is x=10m æ the organ when t=4 iii) Object is slowing when V>0 and a <0 :. 6< t < 8 (between B and C)

2013 APE

Question 16 a) f''(z) = 2 $\frac{1}{(x)} = 2x + c$ $o = 2 \times (+c)$ - 1(=) = 2x-2 1(2) = 2°-2x+k (1,3) 3 = <u>4 = K</u> $f(x) = x^2$ A1=5000 (1.03) -800 4350 $A_2 = A_1 (1.03) - 800$ = 5000 . (1.03) - 800 (1.03) - 800 A3 = 5000 (1.03)3 - 800. (1.03)2 - 800×1.03 - 800 $= 5000 (1.03)^3 - 800 (1 + 1.03 + 1.03^2)$. An = 5000 (1.03) - 800 (1+1.03+1.03 ++1.03 -1 $S_{r} = a(r^{-1})$ 1.03 e are a terms $= 5000 (1.03)^{n} - 800 \left(1 \times (1.03)^{n} - 1 \right)$ $\frac{1}{1.03 - 1}$ $= S_{000} (1.03)^{7} - \frac{800}{0.03} \left[(1.03)^{7} - 1 \right]$ = 5000(1.03)ⁿ - 80000 (1.03)ⁿ + 80000 3 = 1 (80000 + 3×5000 - 80000 (1.03) ~ = 3 [\$ 0000 - 65000 (1.03)]

M4 2013 Question 16 $\frac{6}{3} = \frac{1}{3} \left[\frac{80000 - 65000(1.03)^3}{3} \right]$ = \$2990.915 1.03 $A_{n} = 2790.715(1.03)^{n}$ - 900 $30000 (1.03^{-1}) = 2970.915 (1.03)^{-1}$ $30000 (1.03^{-1}) - 2990.915 (1.03)^{+1} = 30000$ $27009.085(1.03)^{+1} = 30000$ 1.10737 1.03) 2 n= ln 1.110737 In 1.03 - only 3 years left. R=sing $(h-1)^2 + \sin^2 \Theta$ $(h-1)^2 = 1-s_1$ $(h-1)^2 = cos^2 \Theta$ cos 0 +1 = $\frac{V=1}{3}\pi r^{2}h$ $V = \frac{1}{3} \pi \sin^2 \Theta \left(\cos \Theta + 1 \right)$

 $\frac{dv}{d\theta} = \frac{1}{3} \prod \left[\frac{(\cos \theta + 1)}{2\sin \theta \cos \theta} + \sin^2 \theta \left(-\sin \theta \right) \right]$ } $= \frac{\pi}{2} \int 2\sin\theta \cos\theta + 2\sin\theta \cos\theta - \sin^2\theta \int d\theta d\theta$ $\frac{af}{ax} = \frac{1}{16} = 2 \sin \theta \cos^2 \theta + 2 \sin \theta \cos \theta - \sin^2 \theta = \sin^2 \theta \left(2 \cos^2 \theta + 2 \cos \theta - (1 - \cos^2 \theta) \right)$ = Sin 0 [3 cos20 + 20050 -1] $(3\cos\theta - 1)(\cos\theta)$ $\dot{n} \partial = 0$ 11 Test $\Theta = 1$ V is ma 0=1. V1 0.4088 =0 >0 (

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